

*with effect from :2020-21 (R-20)*

**VASAVI COLLEGE OF ENGINEERING (AUTONOMOUS)**

(Accredited by NAAC with A<sup>++</sup> Grade)  
9-5-81, Ibrahimbagh, Hyderabad-500031, Telangana State

**DEPARTMENT OF MATHEMATICS**  
**ADVANCED LINEAR ALGEBRA**  
(OPEN ELECTIVE)

**for B.E., IV- Sem.,**  
(Common to all branches)

Instruction : 3 Hours per week	Sem. End Exam Marks : 60	Subject Reference Code : U20OE410MA
Credits : 3	Sessional Marks : 40	Duration of Semester End Exam : 3 Hrs

COURSE OBJECTIVES	COURSE OUTCOMES
<i>The course will enable the students to:</i>	<i>At the end of the course students will be able to:</i>
<ol style="list-style-type: none"> <li>1. <b>Study</b> the concept of Vector Spaces, Subspaces, Linear Span, Linear Dependence and Independence of vectors.</li> <li>2. <b>Understand</b> the meaning of Basis and Dimension of a vector Space and Co-ordinates.</li> <li>3. <b>Understand</b> the meaning of Linear transformation, properties.</li> <li>4. <b>Understand</b> Range and Kernel, Rank-Nullity and Matrix of Linear Transformation.</li> <li>5. <b>Understand</b> Inner Product Spaces, Orthonormal sets, Gram-Schmidt's Orthogonalization process and its applications :Least squares, QR decomposition</li> </ol>	<ol style="list-style-type: none"> <li>1. <b>Solve the problems</b> on Vector Spaces and Linear Dependence and Independence of vectors.</li> <li>2. <b>Determine</b> the Basis and Dimension of a Vector Space and find the Co-ordinates.</li> <li>3. <b>Determine</b> Linear Transformation, Range and Kernel and Matrix of Linear Transformation.</li> <li>4. <b>Determine</b> Range and Kernel, Rank-Nullity and Matrix of Linear Transformation.</li> <li>5. <b>Determine</b> distance, orthogonal, orthonormal sets and construct orthonormal basis based on Gram-Schmidt's Orthogonalization process. Least Squares approximations-QR decomposition and its applications</li> </ol>

**UNIT –I**

**Vector Spaces -I (8 Hours)**

Internal Composition - External Composition - Definition of Vector Space - Vector Subspaces – Linear sum of two Subspaces – Linear Combination of Vectors – Linear Span of a set - Linear Dependence and Independence of vectors.

**UNIT –II**

**Vector Spaces – II (8 Hours)**

Basis of a Vector Space – Finite Dimensional Space – Coordinates – Dimension of a Vector Space – Dimension of a Subspace-Isomorphism.

### **UNIT-III**

#### **Linear Transformation -I (8 Hours):**

Definition of Linear Transformation- Properties of Linear Transformations – Sum of Linear Transformations – Algebra of Linear Operators

### **UNIT-IV**

#### **Linear Transformation -II (6 Hours)**

Range and kernel of a linear map – Dimension of Range and Kernel - Rank and nullity – Rank nullity theorem (without proof)- Matrix of Linear Transformation.

### **UNIT-V**

#### **Inner Product Spaces (8 classes)**

Definition of Inner Product Space-Norm or Length of a vector -Triangle inequality (with proof)– Normed vector space- Distance – orthogonal complement – Orthogonal and Orthonormal sets – Gram-Schmidt's Orthogonalization process. Applications: Least Squares Approximations-QR decomposition and its applications.

#### **Text Books:**

1. Introduction to linear algebra with applications, Jim DeFranza, Daniel Gagliardi, Tata McGraw-Hill
2. An introduction to Linear Algebra, V.P Mainra, J.L Arora, Affiliated to East-West Press Pvt Ltd

#### **Reference Books:**

1. Elementary Linear algebra, Anton and Rorres, Wiley India Edition
2. Advanced Engineering Mathematics, Erwin Kreysing, Wiley Publication
3. Elementary Linear algebra, ron Larson, Cengage Learning

#### **Online Resources :**

1. <http://tutorial.math.lamar.edu/Classes/DE/DE.aspx>
2. <http://mathworld.wolfram.com/topics>
3. <http://www.nptel.ac.in/course.php>

BS an  
5/3/21